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Published in:
ESANN 2020

Publication date:
2020

Document Version
Peer reviewed version

[Link to publication](#)

Citation for pulished version (HARVARD):

Bibal, A, Vu, VM, Nanfack, G & Frénay, B 2020, Explaining t-SNE embeddings locally by adapting LIME. in *ESANN 2020 : 28th European Symposium on Artificial Neural Networks, Computational Intelligence and Machine Learning*. ESANN (i6doc.com), Bruges, Belgium, pp. 393-398, 28th European Symposium on Artificial Neural Networks, Computational Intelligence and Machine Learning, Bruges, Belgium, 2/10/20.
<<https://dblp.org/db/conf/esann/esann2020.html>>

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Explaining t -SNE Embeddings Locally by Adapting LIME

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Abstract. Non-linear dimensionality reduction techniques, such as t -SNE, are widely used to visualize and analyze high-dimensional datasets. While non-linear projections can be of high quality, it is hard, or even impossible, to interpret the dimensions of the obtained embeddings. This paper adapts LIME to locally explain t -SNE embeddings. More precisely, the sampling and black-box-querying steps of LIME are modified so that they can be used to explain t -SNE locally. The result of the proposal is to provide, for a particular instance \mathbf{x} and a particular t -SNE embedding \mathbf{Y} , an interpretable model that locally explains the projection of \mathbf{x} on \mathbf{Y} .

1 Introduction

An important step in data analysis is to look at the data at hand with the use of dimensionality reduction (DR) techniques. If the dimensionality is reduced to two, the embedding can be presented in a scatter plot and the data can be visually explored. One of the most effective DR techniques is t -SNE [1]. t -SNE is a non-linear DR (NLDR) technique, whose objective is to preserve high-dimensional (HD) neighborhood in the low-dimensional (LD) embedding. While t -SNE is effective to grasp HD patterns visually, the non-parametric mapping is hard to interpret. Moreover, the two dimensions of the embedding may not have a particular meaning [2]. However, as t -SNE preserves neighborhoods, it can be expected that these two dimensions can be analyzed *locally*.

A popular technique for studying black-box models locally through the use of interpretable models is LIME [3]. However, LIME is designed to explain supervised learning models, and is unfortunately not suitable for t -SNE.

In this paper, we propose to drastically change some steps of the LIME algorithm to explain t -SNE and other non-parametric NLDR techniques that need local explanations. The interpretation of t -SNE is discussed in Section 2. LIME is presented and explained in Section 3. The adaption of LIME to locally explain t -SNE embeddings is proposed in Section 4. Results using this new algorithm are shown in Section 5 and the paper is concluded in Section 6.

2 The Interpretability of t -SNE

t -SNE is a non-parametric dimensionality reduction (DR) method that learns embeddings of high-dimensional (HD) data [1]. t -SNE computes pairwise similarities between instances, which are then converted into neighborhood probabilities. Given instances \mathbf{x}_i and \mathbf{x}_j in HD, the probability that they are neighbors is

*The first three authors have contributed equally. G. Nanfack is funded by the EOS VeriLearn project n. 30992574 of the Fonds de la Recherche Scientifique (F.R.S-FNRS) in Belgium.

$p_{ij} = \frac{p_{j|i} + p_{i|j}}{2n}$, where n is the number of instances, $p_{j|i} = \frac{\exp(-\|\mathbf{x}_i - \mathbf{x}_j\|^2 / 2\sigma_i^2)}{\sum_{k \neq i} \exp(-\|\mathbf{x}_k - \mathbf{x}_i\|^2 / 2\sigma_i^2)}$ and σ_i is set by the perplexity. In LD, t -SNE similarly computes pairwise similarities with the Student t -distribution $q_{ij} = \frac{(1 + \|\mathbf{y}_i - \mathbf{y}_j\|^2)^{-1}}{\sum_{k \neq i} (1 + \|\mathbf{y}_k - \mathbf{y}_i\|^2)^{-1}}$, where \mathbf{y}_i is the projection of \mathbf{x}_i in LD. The projections \mathbf{y}_i , $i = 1..n$ are learned by minimizing the Kullback-Leibler (KL) divergence between \mathbf{P} and \mathbf{Q} through gradient descent.

t -SNE achieves state-of-the-art results for dimensionality reduction. Yet, unlike PCA, interpreting the embedding dimensions is difficult or even impossible. Earlier work proposes versions of t -SNE that can be to some extent interpretable. A parametric t -SNE is proposed in [4, 5] as a generalized linear model with an explicit mapping $\mathbf{y}_i = \sum_j \alpha_j K(\mathbf{x}_i, \mathbf{x}_j)$, with K being any kernel. The authors use a Gaussian kernel, which makes the embedding difficult to interpret. Using a linear kernel would make it possible to interpret the mapping, at the expense of losing the non-linear projection quality of t -SNE. More generally, Bunte et al. propose a general framework for DR mappings, that makes it possible to extend DR methods to obtain a (potentially interpretable) explicit mapping [6].

In this paper, we aim to directly explain the non-linear mapping of t -SNE (also called post-hoc interpretability), instead of modifying the method. The challenge is that t -SNE is known for breaking the relationship between instances whose distance is large in HD [2]. Therefore, explaining the embedding globally does not always make sense. As neighborhoods are preserved, we hypothesize that explanations can be made in those very neighborhoods. Using the neighborhood of an instance for a local explanation of a black-box model can be performed by LIME in supervised learning. This paper adapts LIME for t -SNE.

3 LIME for Explaining Models

Local interpretable model-agnostic explanations (LIME) is an algorithm designed to locally explain black-box classifiers and regressors [3]. LIME addresses the question *how a black-box model f behaves in the neighborhood of \mathbf{x}* . To this end, LIME globally samples new samples \mathbf{z}_j around \mathbf{x} and captures the *locality* by weighting the samples \mathbf{z}_j w.r.t. their distance from \mathbf{x} . The black-box model is then queried to get the predictions $f(\mathbf{z}_j)$. An interpretable model, such as a weighted sparse linear model, is used to approximate the behavior of f near \mathbf{x} . While LIME is very popular in supervised learning, very little has been done to use it in unsupervised learning. Because LIME explains locally, it is a good candidate to explain t -SNE embeddings where neighborhoods are preserved.

The LIME algorithm has two phases: sampling new samples \mathbf{z}_j and query the black-box model for predictions $f(\mathbf{z}_j)$. With classical t -SNE, such a query is not possible because no explicit mapping $\mathbf{y}_j = f(\mathbf{z}_j)$ exists. Indeed, if new samples \mathbf{z}_j have to be inserted in an already computed embedding, the embedding must be entirely re-calculated, which means that the whole HD-LD mapping will change. This is an issue because a particular embedding cannot be explained with new instances without being altered. Furthermore, contrarily to LIME, we need to find samples \mathbf{z}_j for which their projection is close to the projection of \mathbf{x} .

In order to implement LIME for t -SNE, three issues must be tackled: (i) the

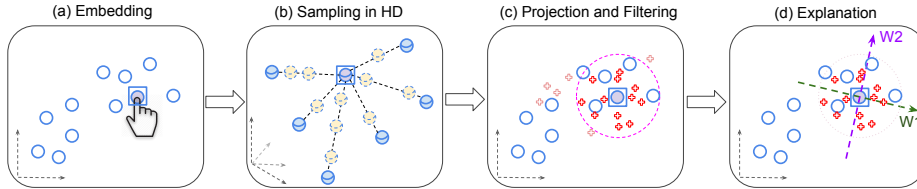


Fig. 1: The proposed workflow for adapting LIME to explain t -SNE embedding.

way new instances are sampled, (ii) the way t -SNE, as a black-box, is queried and (iii) the use of an interpretable model to locally explain t -SNE embeddings.

4 Adapting LIME to Explain t -SNE Embeddings

This section proposes an adaptation of LIME to locally explain t -SNE as illustrated in Fig. 1. Two important changes are introduced: how to sample new instances adequately for t -SNE (Section 4.1) and how to query t -SNE to know how new samples would have been projected (Section 4.2). Finally, an interpretable model for explaining t -SNE locally is presented in Section 4.3.

4.1 Adapting Sampling in LIME for t -SNE

The first contribution of this paper is a sampling strategy to generate samples \mathbf{z}_j to explain a t -SNE embedding around a particular instance \mathbf{x} (see Fig. 1b). The main issue related to the sampling is that the distance between instances that are far apart in HD are not necessarily preserved in LD. In order to solve this issue, several neighbors \mathbf{x}_j of \mathbf{x} in the original dataset are chosen according to the neighborhood size t -SNE used when building the embedding. The SMOTE oversampling [7] is used to produce new samples $\mathbf{z}_j = \mathbf{x} + \alpha * (\mathbf{x}_j - \mathbf{x})$, with $\alpha \in [0, 1]$. Considering new instances between the instance of interest \mathbf{x} and one of its neighbor \mathbf{x}_j , the aim is to obtain a point that fits on the HD manifold.

4.2 Adapting Black-Box Querying in LIME for t -SNE

As explained in Section 3, projecting new samples on an already computed embedding is difficult: t -SNE is non-parametric and the HD-to-LD mapping is unknown. One could use a parametric version of t -SNE [8, 5]. However, this paper focuses on explaining classical t -SNE, instead of modifying to make it interpretable. In order to query t -SNE, we only optimize the projection of each new sample \mathbf{z}_j , while fixing the projection of the instances from the original dataset unchanged (see Fig. 1c). Samples that are projected far away from the projection of \mathbf{x} are filtered out to focus on a local region of the embedding.

When the sampling procedure explained in Section 4.1 is performed and the sampled instances \mathbf{z}_j are projected, the last step is to use an interpretable model to understand the projection of the samples \mathbf{z}_j in the embedding (see Fig. 1d).

4.3 Explaining t -SNE Locally with BIR

t -SNE has particularities that must be taken into account to explain its embeddings with a sparse linear model. t -SNE produces embeddings that are invariant to rotation, as its only purpose is to preserve neighborhoods. Furthermore, clusters inside the embedding are also invariant to rotation to some extent.

This local invariance to rotation means that a linear regression explaining the embedding dimensions locally must find the best orientation of these dimensions. Let \mathbf{X} ($n \times d$) be the original dataset and \mathbf{Y} ($n \times 2$) the embedding, the regression problem is $\mathbf{Y}\mathbf{R} = \mathbf{X}\mathbf{W}$, where \mathbf{R} is a two-dimensional rotation matrix and \mathbf{W} corresponds to the weights of the linear regression model. This is a best interpretable rotation (BIR) problem [9, 10]. The objective of BIR is to find the angle θ^* of \mathbf{R} that provide the best Lasso regression weights \mathbf{W} . Similarly to sparse linear models, BIR involves an hyper-parameter λ that balances the importance of the mean squared error (MSE) with respect to the sparsity.

BIR is run with the best hyper-parameter λ^* found by cross-validation on the sampled data. The result is an angle θ^* and sparse weights \mathbf{W} . The next section shows the interest of the proposed adaption of LIME for t -SNE.

5 Evaluation and Discussion

The proposed method is evaluated on the *Country* dataset [11], which contains 45 socio-economic indicators (e.g. GDP, women in the economy, healthcare, etc.) released in 2007 for 138 countries. The t -SNE visualization is built with a perplexity of 10. Three countries with very different socio-economic characteristics are chosen for the analysis: Spain (Fig. 2a), Bulgaria (Fig. 2b) and Tunisia (Fig. 2c). They are located in different zones of the embedding: Spain at the center of the occidental cluster (top-right of the embedding), Bulgaria and Tunisia at the edge and the center of the largest cluster. For each country, the left-most scatter plot represents the original embedding in blue and the projected samples instances in red. The transparency indicates the errors made by the linear model applied on the original instances, which gives an idea of the zone that can be explained. The scatter plot in the middle is a zoom on the region explained. The right-most figure represents the weights to explain the two local dimensions.

The quasi-horizontal trend centered on Spain (W1 in Fig. 2a) is mainly explained by the GDP PPP (purchasing power parity), the healthcare (e.g. babies immunized to measles) and the number of women in the parliament. On this axis, it can be observed that the country at the far right of W1 is Iceland, a small country that is known for having favored the number of women at the parliament. On the other side of the axis, big countries with an effective economy can be found, such as the USA and Japan. The quasi-vertical trend (W2 in Fig. 2a) is uniquely determined by the aid towards developing countries.

The first axis explaining the trend around Bulgaria (W1 in Fig. 2b) is characterized by economic and political features. Countries towards the right have higher GDP per capita than Bulgaria (\$3109), e.g. Estonia(\$8331), Croatia (\$7724) and Lithuania (\$6480), while countries towards the left receive more refugees than Bulgaria (4k), e.g. Guyana (73k) and Malaysia (34k). The second axis (W2 in Fig. 2b) is a mix of demographic, health and economic features. Towards the top, we find countries with larger expenditure on public health and larger imports of good and services than Bulgaria (4.1% and 69% of GDP) like Malta (7.4% and 83%) and Slovakia (5.2% and 79%), while toward the bottom, countries with smaller population in 1975 than Bulgaria (8.7M) can be found,

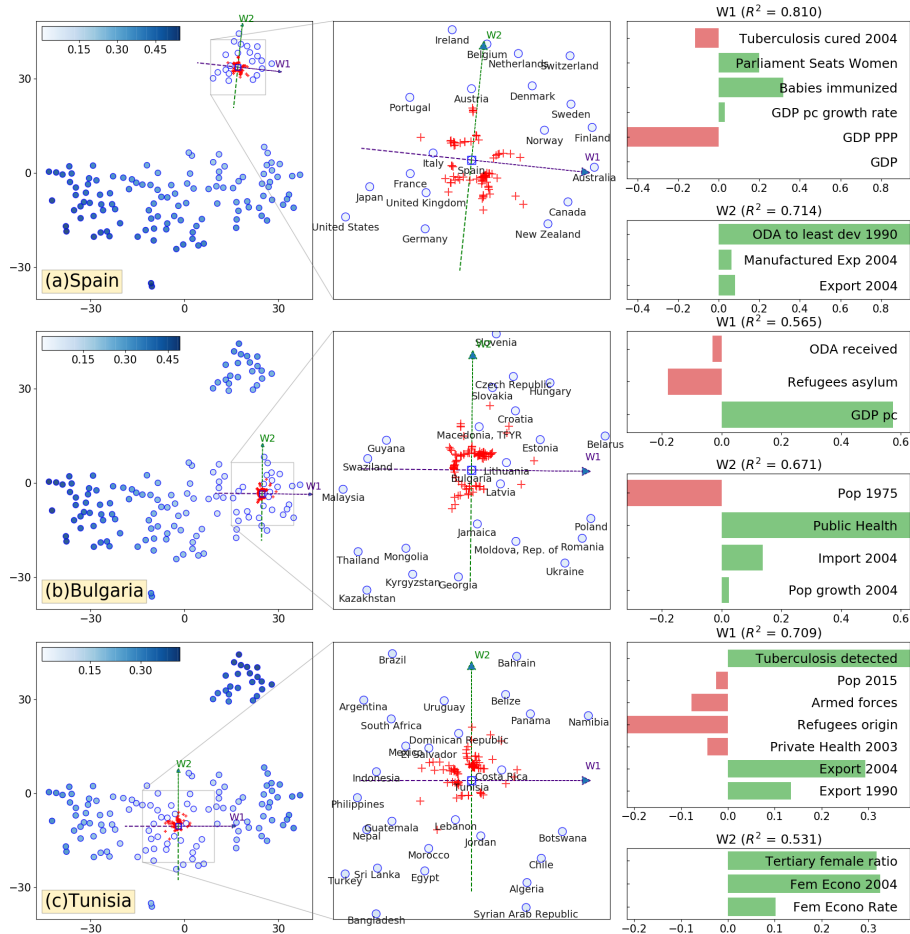


Fig. 2: Evaluation of the proposed method for explaining the local trends in the t -SNE embedding for three selected countries: Spain, Bulgaria and Tunisia. For each axis, R^2 measures how well the embedding is linearly and locally explained. The blue transparency corresponds to the errors of the local model.

like Jamaica (2M), Latvia (2.5M) or Moldova (3.8M).

For the local region around Tunisia on the embedding, the horizontal axis (W1 in Fig. 2c) broadly represents countries that have increased exports from 1990 to 2004, have a rather low population, a small armed force and a high rate of tuberculosis detected in 2004. The countries on the right have a greater rate of tuberculosis detected than Tunisia (96%), e.g. Chile (114%), Panama (133%) and Costa Rica (153%). They also export more than Tunisia (45 % of its GDP in 2004), e.g. Panama (63%) and Costa Rica (46%). In contrast, Indonesia on the left has a much lower export rate of only 31%. The vertical axis (W2 in Fig. 2c) represents the place of women in the economy measured by the ratio of male/female enrolled in the tertiary education, the female economic activity rate

in 2004 and the evolution of the female economic activity rate from 1990 to 2004. Considering the rate of female activity in 2004 and the evolution from 1990 to 2004, in the embedding below Tunisia (with 27.9% and 37%), we see Morocco (26.7% and 33%) and Egypt (20.1% and 28%). Above it, we see Dominican Republic (45.5% and 55%) and Uruguay (55.7% and 71%).

It should be noted that some local regions cannot be explained linearly. For instance, BIR does not find any solution for local regions around Denmark and Lithuania. This can be due to the fact that (i) t -SNE makes mistakes in its projection (i.e. it does not make sense to explain it) and (ii) the mapping can be highly non-linear, so much that it is impossible to explain the region linearly.

6 Conclusion

The main contribution of this paper is to adapt LIME, a method designed to explain any predictive model, in order to explain t -SNE embeddings. First, an oversampling method based on SMOTE is used to generate m relevant samples in HD for a selected instance of interest. Second, only the positions of these m newly created samples are computed by t -SNE. Third, a sparse linear model is used to explain the local orthogonal trends around the selected instance. In future works, the proposed approach will be extended to explain embeddings of image and text datasets. The complexity $O((m+n)^2)$ of the out-of-sample projection can also be improved, e.g. with interpolation [12]. Work can also be done to show where local models are relevant in the visualization.

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